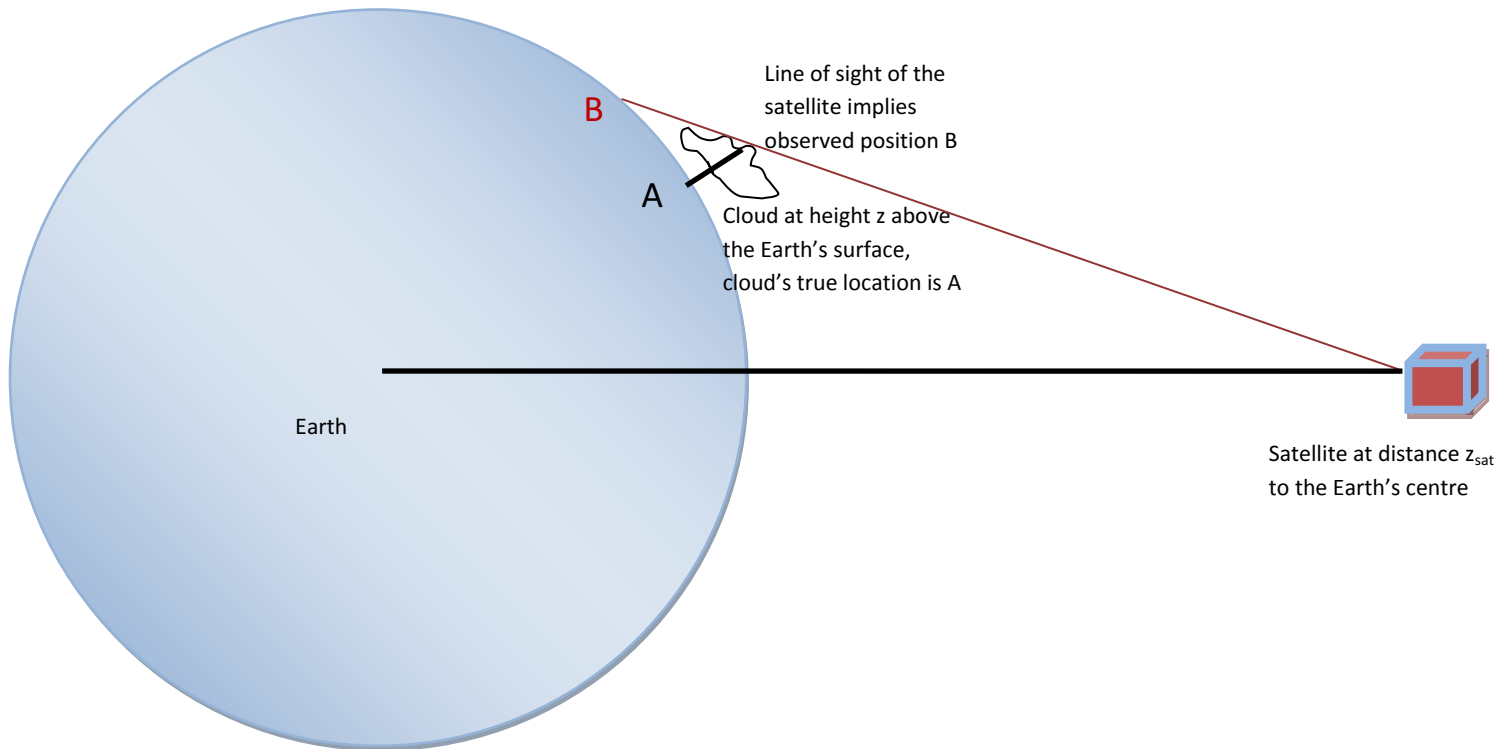


## Description of the parallax correction functionality

A parallax correction to any height (e.g. cloud top height) information is necessary, as the object at height  $h_{\text{cloud}}$ , observed by a satellite at height  $h_{\text{sat}}$  above the Earth's centre, will actually be in a slightly different position than the position recorded by the satellite. The figure below illustrates the concept (not to scale!):



### The parallax correction functionality needs the following input:

Satellite height above the Earth's centre (in km):	$h_{\text{sat}}$
Latitude of subsatellite point:	$\varphi_{\text{sat}}$
Longitude of subsatellite point:	$\lambda_{\text{sat}}$
Height of the observed (cloud) object (in km):	$h_{\text{cloud}}$
Assigned latitude of the object (point B in figure):	$\varphi_{\text{cloud}}$
Assigned longitude of the object (point B in figure):	$\lambda_{\text{cloud}}$

### The parallax correction functionality produces as output:

Parallax corrected latitude of the object (point A in figure):	$\varphi_{\text{cloud,corr}}$
Parallax corrected longitude of the object (point B in figure):	$\lambda_{\text{cloud,corr}}$

### The following static data are needed:

Earth radius, equator (in km):	$R_{\text{equ}}$
Earth radius, pole (in km):	$R_{\text{pole}}$
Mean Earth radius (in km):	$R_{\text{mean}} = 0.5 (R_{\text{equ}} + R_{\text{pole}})$
Radius ratio:	$R_{\text{ratio}} = R_{\text{equ}} / R_{\text{pole}}$

Note: Latitude  $\varphi$  is defined between  $-90^\circ$  and  $+90^\circ$  (resp. between  $-\pi/2$  and  $+\pi/2$  if expressed in radians), latitudes North are positive. Longitude  $\lambda$  is defined between  $-180^\circ$  and  $+180^\circ$  (resp. between  $-\pi$  and  $+\pi$  if expressed in radians), longitudes East are positive.

Note: The earth radii  $R_{\text{equ}}$  and  $R_{\text{pole}}$  should have the same values as used elsewhere in the L1/L2 processing

### Step 1: Express satellite position in Cartesian coordinates

$$x_{\text{sat}} = h_{\text{sat}} \cos(\varphi_{\text{sat,geod}}) \sin(\lambda_{\text{sat}})$$

$$y_{\text{sat}} = h_{\text{sat}} \sin(\lambda_{\text{sat}})$$

$$z_{\text{sat}} = h_{\text{sat}} \cos(\varphi_{\text{sat,geod}}) \cos(\lambda_{\text{sat}})$$

where  $\varphi_{\text{sat,geod}}$  is the geodetic latitude of the subsatellite point, defined as

$$\varphi_{\text{sat,geod}} = \arctan \left[ \tan(\varphi_{\text{sat}}) R_{\text{ratio}}^2 \right]$$

sin, cos, tan, arctan are the trigonometric sine, cosine, tangent and inverse tangent functions.

### Step 2: Express the surface position of point B in Cartesian coordinates

$$x_{\text{cloud}} = R_{\text{local}} \cos(\varphi_{\text{cloudgeod}}) \sin(\lambda_{\text{cloud}})$$

$$y_{\text{cloud}} = R_{\text{local}} \sin(\lambda_{\text{cloud}})$$

$$z_{\text{cloud}} = R_{\text{local}} \cos(\varphi_{\text{cloudgeod}}) \cos(\lambda_{\text{cloud}})$$

where  $R_{\text{local}}$  is the Earth's radius at point B, and  $\varphi_{\text{cloudgeod}}$  is the geodetic latitude of point B, according to

$$R_{\text{local}} = \frac{R_{\text{eq}}}{\sqrt{\cos^2(\varphi_{\text{cloudgeod}}) + R_{\text{ratio}}^2 \sin^2(\varphi_{\text{cloudgeod}})}}$$

$$\varphi_{\text{cloudgeod}} = \arctan \left[ \tan(\varphi_{\text{cloud}}) R_{\text{ratio}}^2 \right]$$

**Step 3: Compute local ratio of Earth radii, corrected for cloud top height (squared)**

$$R_{\text{ratio,local}} = \left( \frac{R_{\text{equ}} + h_{\text{cloud}}}{R_{\text{pole}} + h_{\text{cloud}}} \right)^2$$

**Step 4: Compute the difference vector between the satellite and the cloud (point B) position**

$$x_{\text{diff}} = x_{\text{sat}} - x_{\text{cloud}}$$

$$y_{\text{diff}} = y_{\text{sat}} - y_{\text{cloud}}$$

$$z_{\text{diff}} = z_{\text{sat}} - z_{\text{cloud}}$$

**Step 5: Compute the correction for the line of sight at the cloud top height  $h_{\text{cloud}}$**

$$c = \frac{\sqrt{e_2^2 - 4e_1e_3} - e_2}{2e_1}$$

with

$$e_1 = x_{\text{diff}}^2 + R_{\text{ratio,local}} y_{\text{diff}}^2 + z_{\text{diff}}^2$$

$$e_2 = 2(x_{\text{cloud}} x_{\text{diff}} + R_{\text{ratio,local}} y_{\text{cloud}} y_{\text{diff}} + z_{\text{cloud}} z_{\text{diff}})$$

$$e_3 = x_{\text{cloud}}^2 + R_{\text{ratio,local}} y_{\text{cloud}}^2 + z_{\text{cloud}}^2 - (R_{\text{equ}} + h_{\text{cloud}})^2$$

**Step 6: Apply correction to Cartesian coordinates of cloud position (point B)**

$$x_{\text{corr}} = x_{\text{cloud}} + c x_{\text{diff}}$$

$$y_{\text{corr}} = y_{\text{cloud}} + c y_{\text{diff}}$$

$$z_{\text{corr}} = z_{\text{cloud}} + c z_{\text{diff}}$$

$x_{\text{corr}}$ ,  $y_{\text{corr}}$  and  $z_{\text{corr}}$  are now the Cartesian coordinates of the parallax corrected location (point A in figure).

**Step 7: Convert corrected Cartesian coordinates back to latitude and longitude (of point A)**

$$\varphi_{\text{cloudcorr}} = \arctan \left[ \frac{\tan \left( \arctan \frac{y_{\text{corr}}}{\sqrt{x_{\text{corr}}^2 + z_{\text{corr}}^2}} \right)}{R_{\text{ratio}}^2} \right]$$

$$\tan(\lambda_{\text{cloudcorr}}) = \frac{x_{\text{corr}}}{z_{\text{corr}}}$$

The corrected longitude  $\lambda_{\text{cloud,corr}}$  can then in principle derived through the inverse tangent function, but care has to be given as to the actual quadrant of the 360° circle. In any modern computer language, this is easily achieved by the ATAN2 function, which is given two arguments:

$$\lambda_{\text{cloudcorr}} = \text{ATAN2}(x_{\text{corr}}, y_{\text{corr}})$$

**Example removed.**